



Model Answer 12th Week Exam

Answer the following questions:

1. For ideal flow of water as shown in the below Figure, the mass flow rate is 8.83 kg/s. Find the manometer reading (y) and the absolute pressure (P₁). The atmospheric pressure is 101.3 kPa.

$m = 8.83 \text{ Kg/sec} = \rho Q$

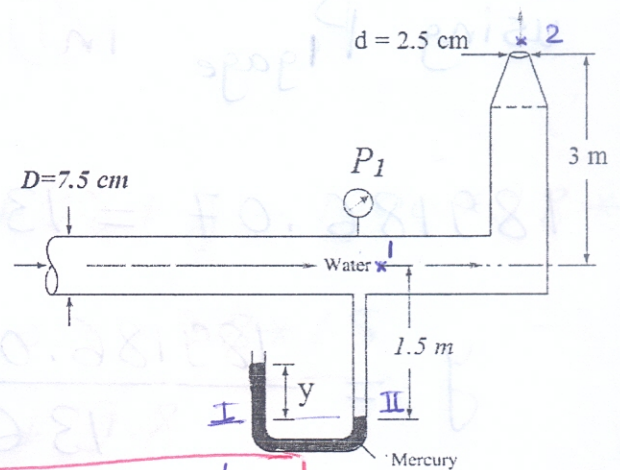
$Q = \frac{8.83}{1000} = 8.83 \times 10^{-3} \text{ m}^3/\text{sec}$

C.E. $Q = A_1 V_1 = A_2 V_2$

$8.83 \times 10^{-3} = \frac{\pi}{4} (7.5 \times 10^{-2})^2 V_1$
 $= \frac{\pi}{4} (2.5 \times 10^{-2})^2 V_2$

$V_1 = 1.999 \text{ m/sec}$

$V_2 = 17.988 \text{ m/sec}$



from u-tube manometer

$P_I = P_{II}$

$P_{atm} + \rho_m g y = \rho_w g \cdot 1.5 + P_1$

$\therefore P_1 = \rho_m g y - \rho_w g \cdot 1.5$

$= 13600 \cdot 9.8 \cdot y - 1000 \cdot 9.8 \cdot 1.5 \rightarrow \textcircled{1}$

B.E. 1 → 2

$E_1 = E_2$

$\frac{P_1}{\rho g} + z_1 + \frac{V_1^2}{2g} = \frac{P_2}{\rho g} + z_2 + \frac{V_2^2}{2g}$

$\frac{P_1}{1000 \cdot 9.8} + \frac{(1.999)^2}{2 \cdot 9.8} = 3 + \frac{(17.988)^2}{2 \cdot 9.8}$

$$P_1 = 189186.07 \text{ Pa}$$

$$P_{\text{abs}} = P_1 + P_{\text{atm}}$$

$$= 189186.07 + 101.3 \times 10^3$$

$$= 290486.07 \text{ Pa abs}$$

$$P_{\text{abs}} = 2.9 \text{ bar abs}$$

using P_{gage} in eqn ①

$$189186.07 = 13600 \times 9.8 \times y - 1000 \times 9.8 \times 1.5$$

$$y = \frac{189186.07 + 1000 \times 9.8 \times 1.5}{13600 \times 9.8}$$

$$= 1.529757$$

$$y = 1.53 \text{ m}$$

①

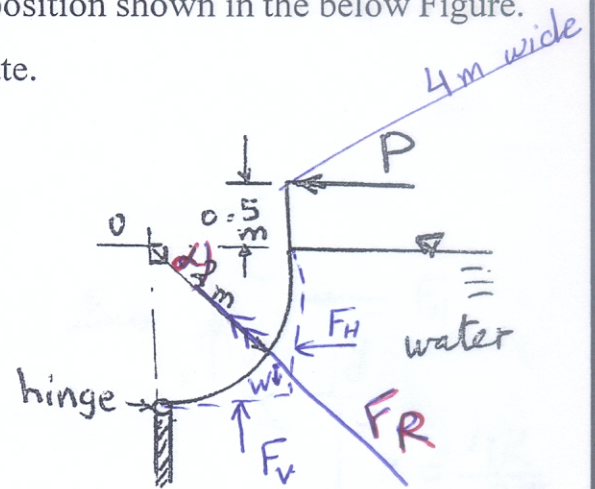
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Reg. No.:

2. Find the force (P) required to hold the gate in the position shown in the below Figure.

The gate is 4 m wide. Neglect the weight of the gate.

$$\begin{aligned}F_H &= \rho g \left(s + \frac{b}{2} \right) ab \\&= \rho g a \frac{b^2}{2} \\&= 1000 * 9.8 * 4 * \frac{2^2}{2} \\&= 78400 \text{ Newton}\end{aligned}$$



$$\begin{aligned}F_V &= \rho g h A \\&= 1000 * 9.8 * 2 * 2 * 4 = 156800 \text{ N}\end{aligned}$$

$$\begin{aligned}W &= \rho g V \\&= 1000 * 9.8 * \left[\square + \text{D} \right] * 4 \\&= 9800 * \left[2^2 - \frac{1}{4} * \pi 2^2 \right] * 4 \\&= 33649.568 \text{ Newton}\end{aligned}$$

$$\begin{aligned}\rho &= \frac{m}{V} \\mg &= \rho V g\end{aligned}$$

$$F_y = F_V - W = 123150.432 \text{ N}$$

$$F_R = \sqrt{F_x^2 + F_y^2} = 145988.3177 \text{ N}$$

$$\alpha = \tan^{-1} \frac{F_y}{F_x} = 57.52^\circ$$

$$\sum M_{\text{hinge}} = 0 \quad (+\uparrow)$$

$$F_R \cos \alpha * 2 + P * 2.5 = 0$$

$$\begin{aligned}P &= -62720 \text{ Newton} \\&= -62.72 \text{ KN}\end{aligned}$$

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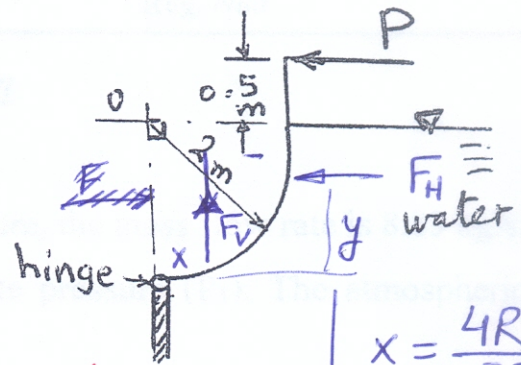
Another solution

Reg. No.:

2. Find the force (P) required to hold the gate in the position shown in the below Figure.

The gate is 4 m wide. Neglect the weight of the gate.

$$\begin{aligned} F_H &= \rho g h_c A \\ &= 1000 \times 9.8 \times 1 \times (2 \times 4) \\ &= 78400 \text{ N} \end{aligned}$$



$$\begin{aligned} F_V &= \rho g * \text{wide} * A = \delta \text{ \textit{missing Fluid}} \\ &= 1000 * 9.8 * 4 * \left(\frac{\pi}{4} * 2^2\right) \\ &= 123150.43 \text{ N} = 39200\pi \text{ N} \end{aligned}$$

$$\begin{aligned} x &= \frac{4R}{3\pi} \\ &= \frac{4 * 2}{3\pi} \\ y &= \frac{R}{3} \\ &= \frac{2}{3} \end{aligned}$$

$$\sum M_{\text{hinge}} = 0$$

$$F_V x + F_H y + P * 2.5 = 0$$

$$123150.43 * \frac{8}{3\pi} + 78400 * \frac{2}{3} + P * 2.5 = 0$$

$$P = -62.793 \text{ N}$$