

## Losses in pipes

### Types of losses

#### 1 – Friction losses :

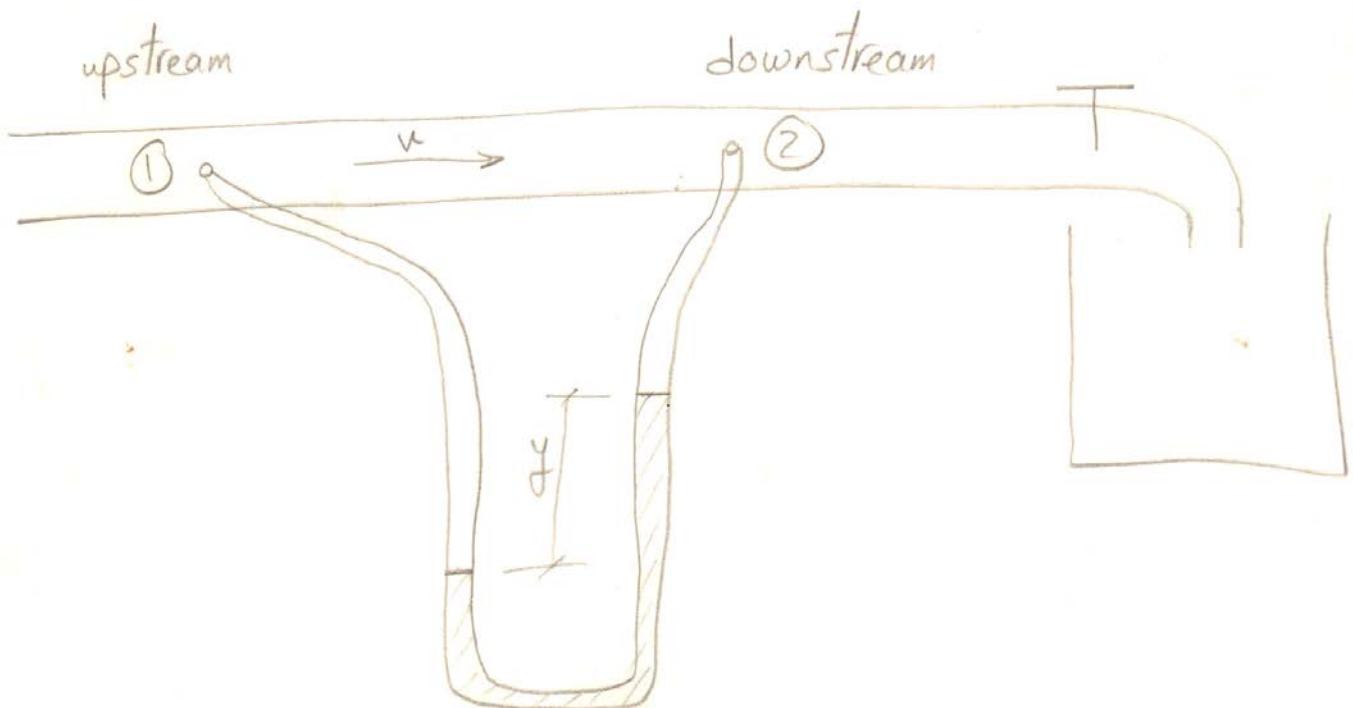
This type of losses exists for any flow as a result of fluid viscosity and velocity difference between fluid layers. As a result of friction, part of the fluid's mechanical energy is converted into heat energy (dissipated into atmosphere) and is considered as an energy loss.

#### 2 – Eddy losses :

This type of losses occurs due to any change in the velocity vector (magnitude or direction). This change causes some of energy to be transferred from main flow to eddies formed at corners. This part of energy is considered as energy losses.

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\* **Friction losses** ماسورة ليس بها تغيير بالمساحة لحساب



$$E_1 = E_2 + h_{loss1to2}$$

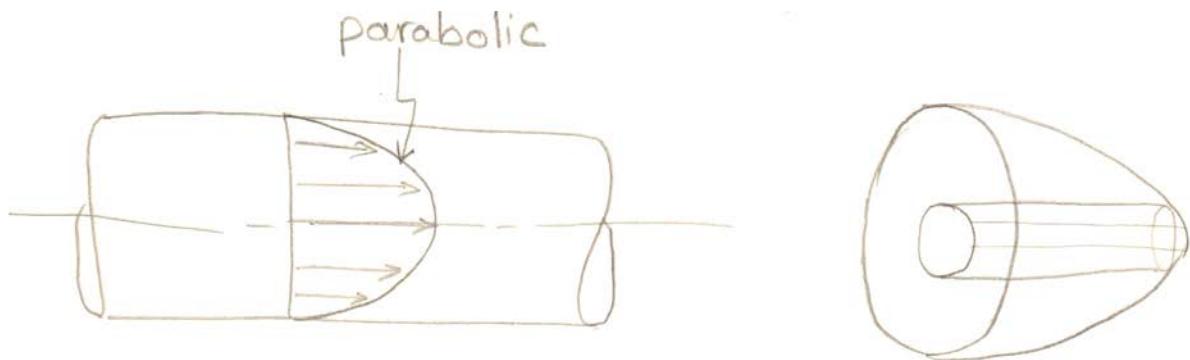
$$\frac{P_1}{\rho g} + z_1 + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + z_2 + \frac{v_2^2}{2g} + h_{loss1to2}$$

$$\frac{P_1}{\rho g} = \frac{P_2}{\rho g} + h_{loss1to2}$$

$$h_{f.l.} = \frac{P_1 - P_2}{\rho g} \quad \text{----- (1)}$$

تم تسميتها  $h_{f.l.}$  لأنها كلها friction losses وليس بها eddy losses

### \* Friction losses in laminar flow Re < 2000



Velocity distribution for laminar flow

$$F_{vis} = \mu A \frac{du}{dy} \quad \text{----- (2)}$$

From (1) & (2)

$$h_{f.l.} = \frac{32\mu v L}{\rho g d^2}$$

Where L is the pipe length

$$h_{f.l.} \propto v \quad (\text{linear})$$

$$h_{f,l} = 32 * \frac{\mu v L}{\rho g d^2} * \frac{v}{\nu} * \frac{2}{2}$$

$$= 32 * 2 * \frac{\mu}{\rho v d} * \frac{L}{d} \frac{v^2}{2g}$$

$$= \frac{64}{R_e} * \frac{L}{d} \frac{v^2}{2g}$$

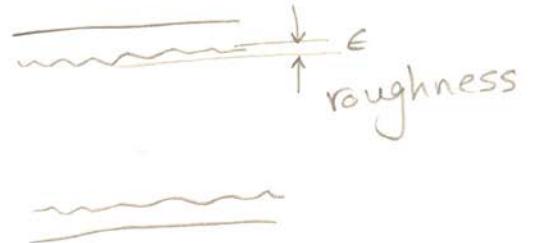
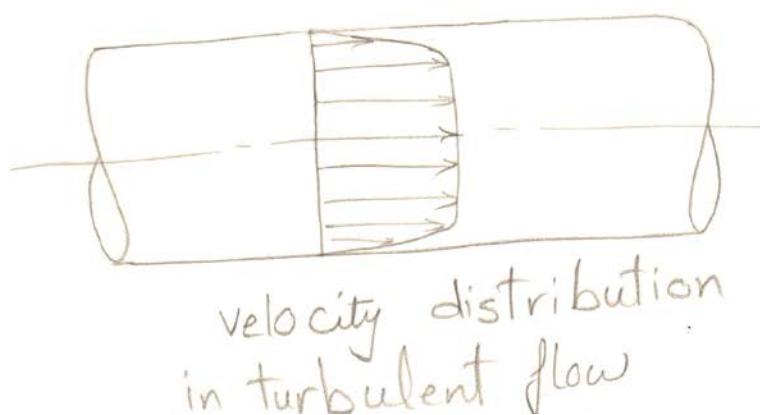
$$h_{f,L} = f \frac{L}{d} \frac{v^2}{2g} \rightarrow$$

Another from  $f = \frac{64}{R_e}$  where f : coefficient of friction

### Note :

for laminar flow , the pipe roughness has no effect on friction losses because the velocity of the fluid layer beside the pipe wall is very small and almost stationary.

### B – friction losses in turbulent flow $Re > 4000$

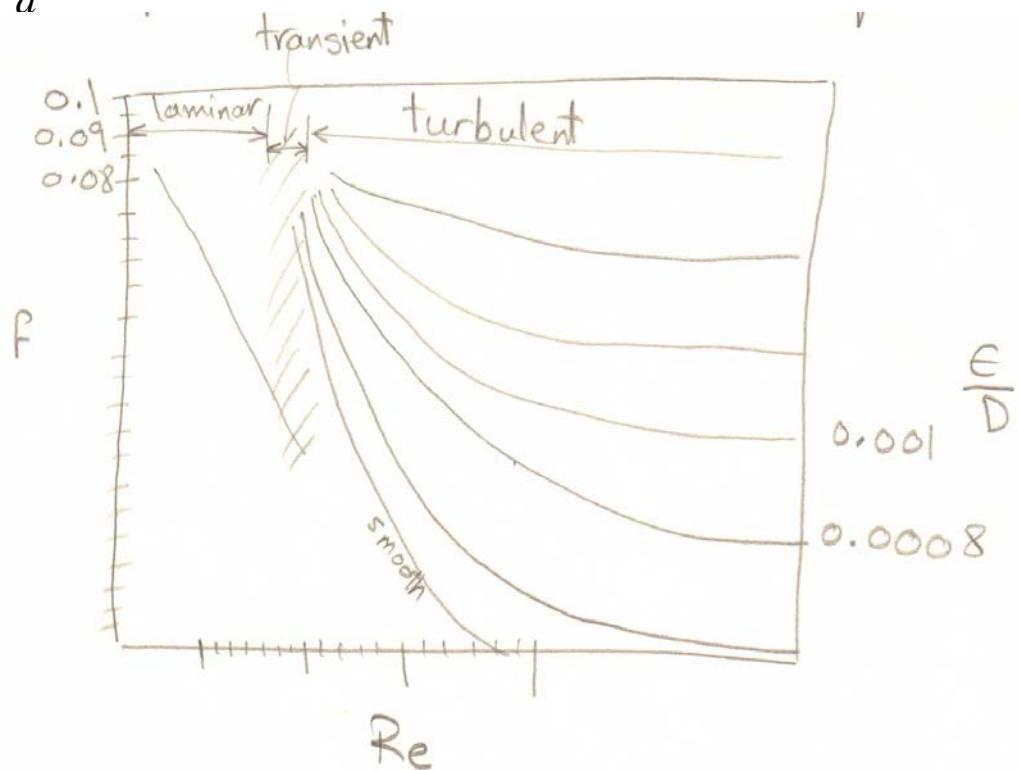


\* All the following results are experimental results written as empirical formula

$$h_{f,l} = f \frac{L}{d} \frac{v^2}{2g}$$

$$h_{f,l} \propto v^2$$

$$F \left\{ \begin{array}{l} Re = \frac{\rho v d}{\mu} \\ \frac{\varepsilon}{d} \end{array} \right.$$

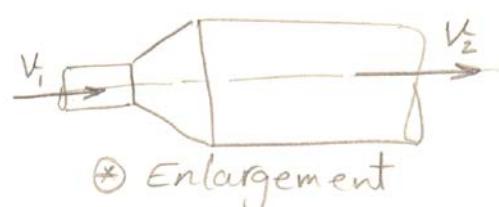
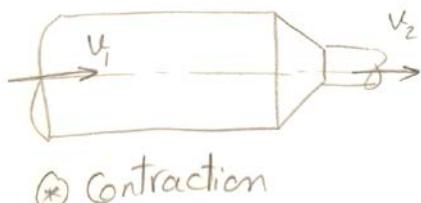


### \*Eddy losses :

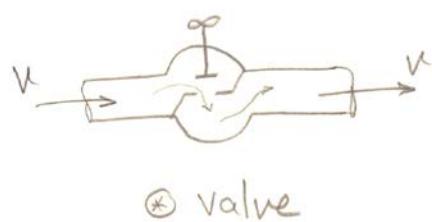
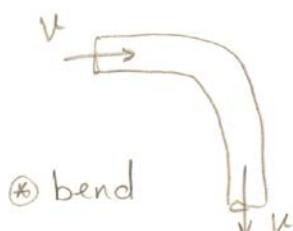
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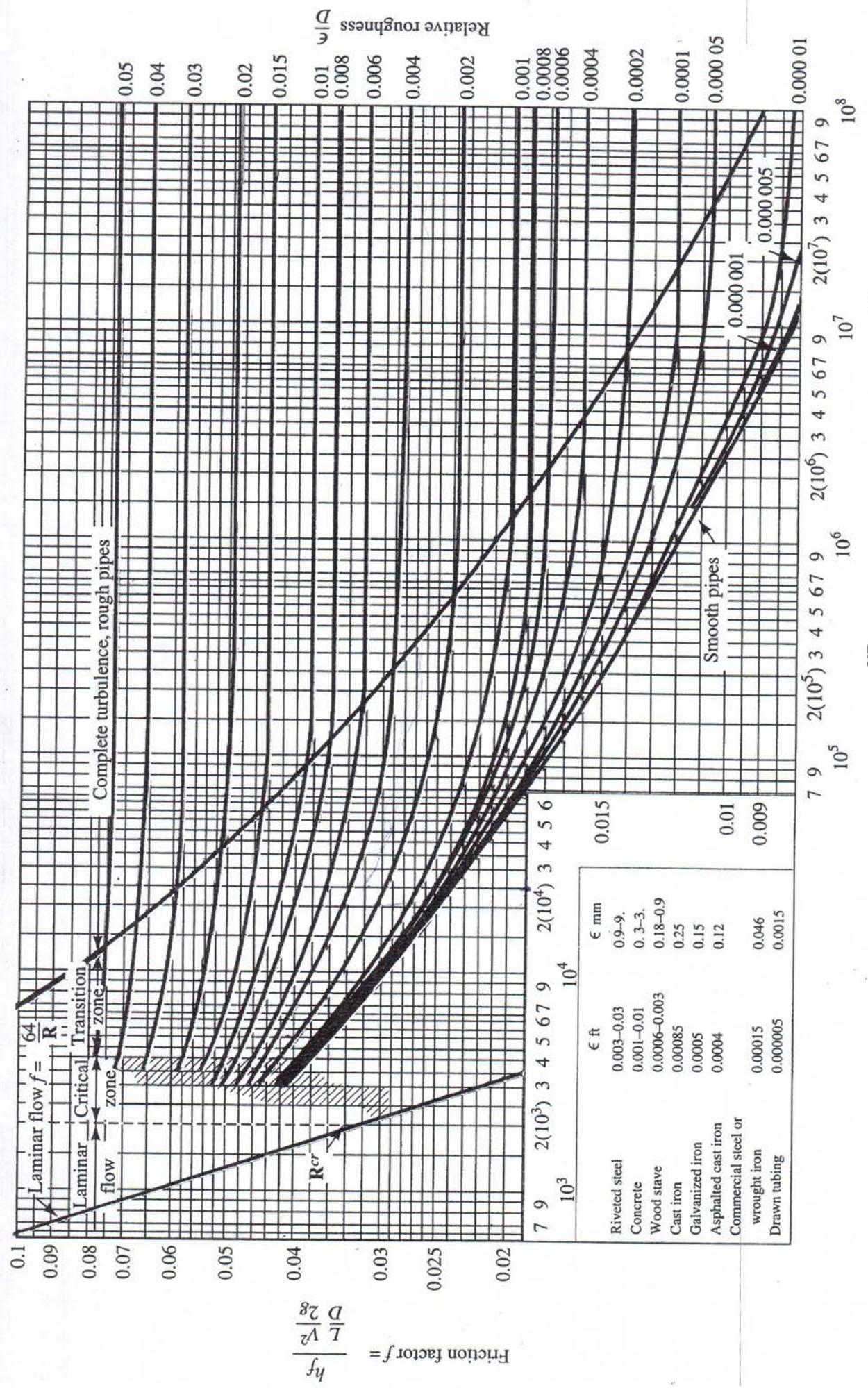
All eddy losses depend only on kinetic energy ( $\frac{v^2}{2g}$ ) of flow (not type of flow).

### I – change in magnitude



### II – change in direction





Reynolds number  $R = \frac{VD}{\nu}$ , consistent units

### \* contraction

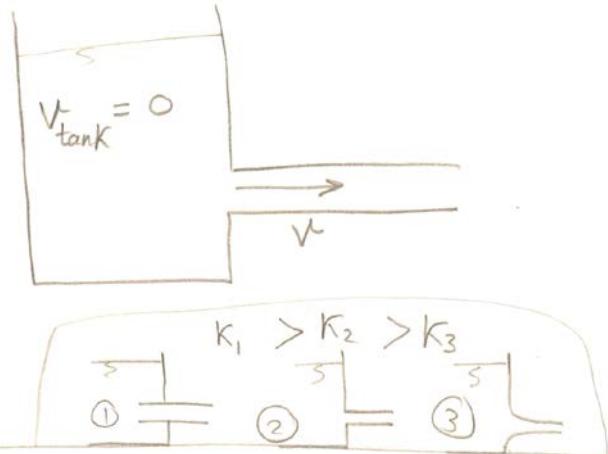
$$h_e = K \frac{V_2^2}{2g}$$

$K$ : Coefficient of eddy loss  
 $K = f_n(\frac{d_1}{d}, \theta)$

$$\text{at } \frac{d_1}{d_2} = \infty \quad \& \quad \theta = 90^\circ$$

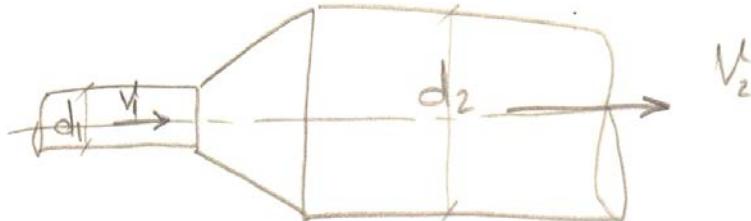
$$k_{\max} = 0.5$$

$$h_e = 0.5 \frac{v^2}{2g}$$



### \* Enlargement

$$h_e = k \frac{(v_1 - v_2)^2}{2g}$$



$k = f_n(\theta)$  The effect of  $\frac{d_2}{d_1}$  is presented in  $(v_1 - v_2)$

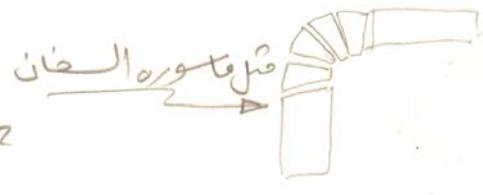
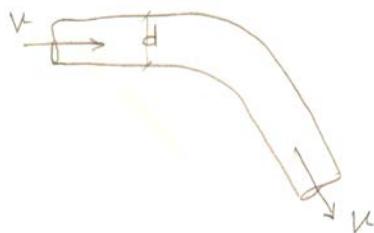
$k_{\max}$  For enlargement at  $\theta = 90^\circ$

(sudden enlargement)

$$k_{\max} = 1$$

$$h_e = \frac{(v_1 - v_2)^2}{2g}$$

### \* Bend or Elbow

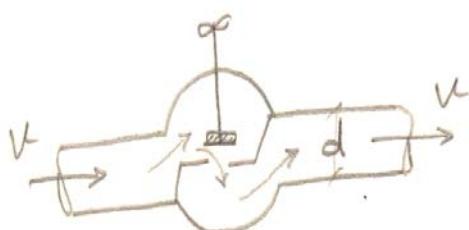


$$h_\ell = k \frac{v^2}{2g}$$

$k = fn(\theta, d, \text{type of bend})$

### \* valves

#### Globe valve



$$h_\ell = k \frac{v^2}{2g}$$

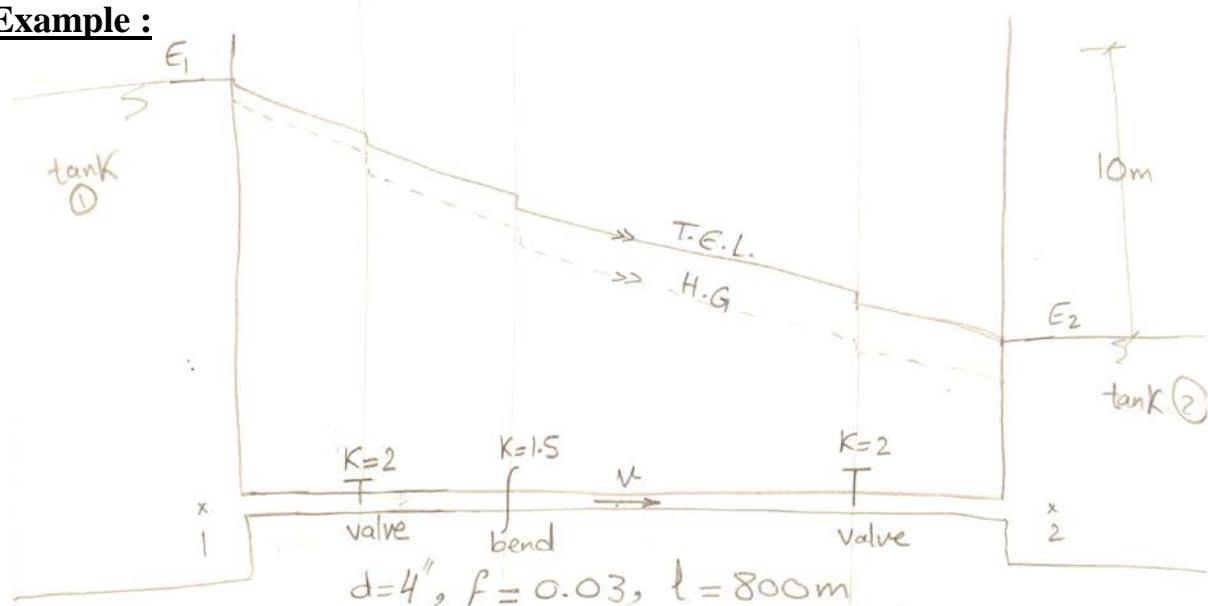
$k = fn(d, \text{type of valve})$

Only for fully opened valves

-عند غلق المفاتيس نصف يكون هناك فاقد اكبر في الطاقة

-لذلك الاستخدام الامثل لها ان تكون مفتوحة بالكامل او مغلقة بالكامل

### Example :



- Calculate the discharge between the tanks.
- One of valves is partially closed. The discharge reduced by 50 %. calculate the losses in the valve in this case.

$$a) \quad d = \frac{4 * 2.54}{100} = 0.1m$$

$$Q = A V$$

$$E_1 = E_2 + h_{loss}$$

$$10 = f \frac{\ell}{d} \frac{v^2}{2g} + k_{ent} \frac{v^2}{2g} + K_v \frac{v^2}{2g} + K_b \frac{v^2}{2g} + K_v \frac{v^2}{2g} + K_{ent} \frac{(v - o)^2}{2g}$$

$$10 = \frac{v^2}{2 * 9.8} (0.03 * \frac{800}{0.1} + 0.5 + 2 + 1.5 + 2 + 1)$$

$$V = 0.89m/s$$

$$Q = 7 \times 10^{-3} \text{ m}^3/\text{s}$$


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b)

$$Q = 0.5Q = A v^1$$

$$\therefore 10^{-3} * 3.5 = \frac{\pi}{4} (0.1)^2 V_1$$

$$V_1 = 0.445m/s$$

$$E_1 - E_2 = h_{loss} = 10$$

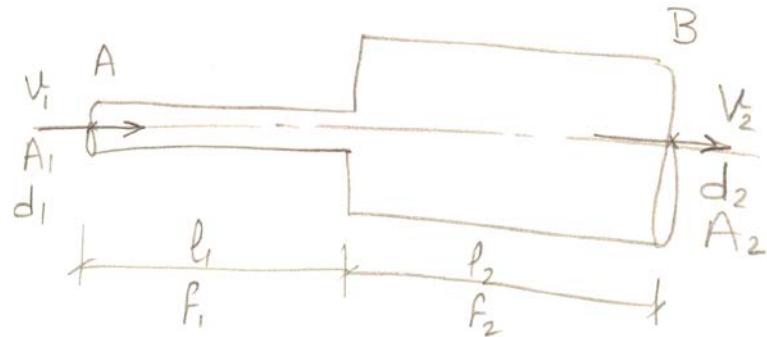
$$10 = f \frac{\ell}{d} \frac{v_1^2}{2g} + k_{ent} \frac{v_1^2}{2g} + h_{loss} + K_b \frac{v_1^2}{2g} + K_v \frac{v_1^2}{2g} + K_{max} \frac{v_1^2}{2g}$$

$$10 = 0.03 * \frac{800}{0.1} + \frac{(0.445)^2}{2 * 9.8} 0.5 \frac{(0.445)^2}{2 * 9.8} + h_{loss} 2 + 1.5 + \frac{(0.445)^2}{2 * 9.8} + 2 + \frac{(0.445)^2}{2 * 9.8} + \frac{1 * (0.445 - o)^2}{2 * 9.8}$$

$$H_{loss} = 7.5 \text{ m of liquid}$$


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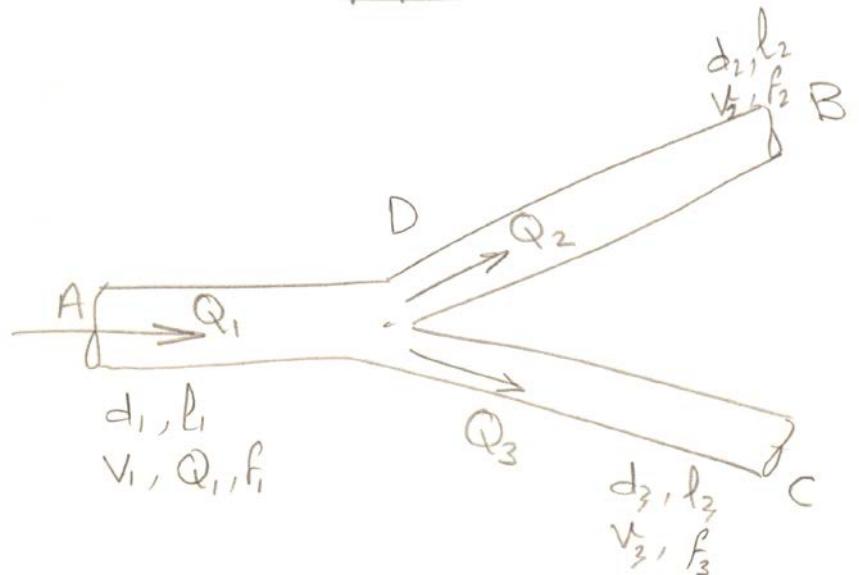
**\* losses in series pipes :**



$$h_\ell = f_1 \frac{\ell_1 v_1^2}{d_1 2g} + \frac{K(v_1 - v_2)^2}{2g} + f_2 \frac{\ell_2 v_2^2}{d_2 2g}$$


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**\* losses in parallel pipes**



$$h_{\ell_{A \rightarrow B}} = f_1 \frac{\ell_1 v_1^2}{d_1 2g} + h\ell_{branching} + f_2 \frac{\ell_2 v_2^2}{d_2 2g}$$

$$h_{\ell_{A \rightarrow C}} = f_1 \frac{\ell_1 v_1^2}{d_1 2g} + h\ell_{branching} + f_3 \frac{\ell_3 v_3^2}{d_3 2g}$$

$$Q_1 = Q_2 + Q_3$$

$$A_1 V_1 = A_2 V_2 + A_3 V_3$$