



College of Engineering & Technology

Department: Mechanical Engineering Marks: 15
Lecturer: Dr. Rola Afify Time: 3.00 - 4.00
Course Code: ME356 Date: 11/11/2015

Name: Model Answer

R.N.:

Answer the following questions:

Question one (6 marks)

A shaft 40 mm diameter is made from steel and the maximum allowable shear stress for the material is 50 MPa. Calculate the maximum torque that can be safely transmitted by the shaft. Take $G = 90$ GPa.

$$d = 40 \text{ mm}$$

$$\tau_{\text{max all}} = 50 \text{ MPa}$$

$$T_{\text{max}} = ??$$

sol'n

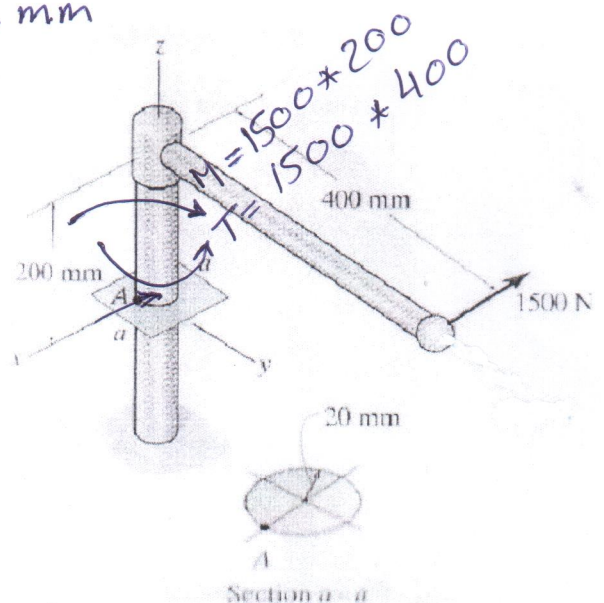
$$\tau = \frac{Tr}{J} = \frac{T_{\text{max}} * 20}{\frac{\pi}{32} (40)^4} = \tau_{\text{max all}}$$

$$50 = \frac{20 T_{\text{max}}}{251327.4}$$

$$T_{\text{max}} = 628318.53 \text{ N}\cdot\text{mm}$$

$$= 628.3 \text{ N}\cdot\text{m}$$

$$= 200 \pi \text{ N}\cdot\text{m}$$



Question two (9 marks)

Determine the maximum stress at section a-a shown in Figure.

$$\begin{aligned} \text{Torsion} \quad \tau &= \frac{Tr}{J} = \frac{1500 * 400 * 20}{\frac{\pi}{32} (40)^4} \\ &= 47.75 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Bending} \quad \sigma_b &= \frac{My}{I} = \frac{1500 * 200 * 20}{\frac{\pi}{64} (40)^4} \\ &= 47.75 \text{ MPa} \end{aligned}$$

The stresses are from different kinds

$$\begin{aligned} \sigma_{\max} &= \frac{\sigma_b}{2} + \sqrt{\left(\frac{\sigma_b}{2}\right)^2 + \tau^2} \\ &= \frac{47.75}{2} + \sqrt{\left(\frac{47.75}{2}\right)^2 + (47.75)^2} \\ &= 77.26 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \tau_{\max} &= \sqrt{\left(\frac{\sigma_b}{2}\right)^2 + \tau^2} \\ &= \sqrt{\left(\frac{47.75}{2}\right)^2 + (47.75)^2} \\ &= 53.386 \text{ MPa} \end{aligned}$$