

Question (1)

$$F = 2000 \text{ N} \quad n = 5 \quad \tau_{\max} = 150 \text{ MPa} \quad L = 240 \text{ mm}$$

$d_{\min} ?$

_____ sol _____

$$T = F \times L = 2000 \times 240 = 480 \times 10^3 \text{ N.mm}$$

$$T = 4 F_s r_1 \quad (\text{as } r_1 = r_2 = r_3 = r_4)$$

$$r_1 = 20\sqrt{2} \text{ mm}$$

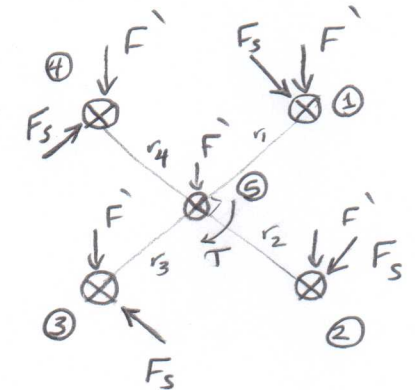
$$F_s = \frac{T}{4 r_1} = \frac{480 \times 10^3}{4 \times 20\sqrt{2}}$$

$$F_s = 4242.6 \text{ N}$$

primary shear

$$F' = \frac{F}{n} = \frac{2000}{5}$$

$$F' = 400 \text{ N}$$



$$\theta = 45^\circ$$

max stress on ① or ②

$$F_{\text{total}} = \sqrt{F'^2 + F_s^2 + 2 F' F_s \cos \theta}$$

$$F_{\text{total}} = \sqrt{(4242.6)^2 + (400)^2 + 2 \times 4242.6 \times 400 \cos 45}$$

$$F_{\text{total}} = 4534.3 \text{ N}$$

$$\therefore \tau_{\max} = \frac{F_{\text{total}}}{A_{\text{bolt}}} = \frac{F_{\text{total}}}{\frac{\pi}{4} d_i^2} \Rightarrow 150 = \frac{4534.3}{\frac{\pi}{4} d_i^2}$$

$$d_i = 6.2 \text{ mm} \Rightarrow d_i = 0.85 d_o \Rightarrow d_o = 7.3 \text{ mm} \quad d_o = 8 \text{ mm}$$

if $L \downarrow \quad T \downarrow \quad F_s \downarrow \quad F_{\text{total}} \downarrow \quad \therefore A_{\text{bolt}} \downarrow \quad d_o \downarrow$

Question (2)

$$n=1 \quad d_m = 50 \text{ mm} \quad P = 12.5 \text{ mm} = L \quad W = 10 \times 10^3 \text{ N}$$

$$d_c = 60 \text{ mm} \quad \mu = 0.15 \quad \mu_c = 0.18 \quad f = 100 \text{ N}_{\text{handle}}$$

Req: D_{wheel} ? , η ? , check ?

_____ sol _____

for square threads $\alpha = \text{Zero}$ $\sec \alpha = 1$

$$T = W \times \frac{d_m}{2} \left[\frac{\pi \mu d_m + L}{\pi d_m - \mu L} \right] + \frac{\mu_c W d_{mc}}{2}$$

$$T = 10 \times 10^3 \times \frac{50}{2} \left[\frac{\pi \times 0.15 \times 50 + 12.5}{\pi \times 50 - 0.15 \times 12.5} \right] + \frac{0.18 \times 10 \times 10^3 \times 60}{2}$$

$$T = 58087.7 + 54000$$

$$\boxed{T = 112.1 \times 10^3 \text{ N.mm}}$$

$$T_o = \frac{WL}{2\pi} = \frac{10 \times 10^3 \times 12.5}{2\pi} \Rightarrow \boxed{T_o = 19.9 \times 10^3 \text{ N.mm}}$$

$$\eta = \frac{T_o}{T} = \frac{19.9 \times 10^3}{112.1 \times 10^3} \Rightarrow \boxed{\eta = 17.8 \%}$$

$$\because T = f_{\text{handle}} \times L_{\text{handle}} \Rightarrow L_{\text{hand}} = \frac{112.1 \times 10^3}{100} = 1121 \text{ mm}$$

$$\boxed{L_{\text{hand}} = 1.12 \text{ m}}$$

check

$$\pi d_m \mu = \pi \times 50 \times 0.15 = 23.6 \text{ mm}$$

$$\because L < \pi d_m \mu \quad (\text{self locking}) (\text{overhauling})$$

Question (3) $\tau_{max} = 120 \text{ MPa}$, $h = 6 \text{ mm}$

Max stress on C or F as r_{max} & θ_{min}
from table $b = 80 \text{ mm}$, $d = 60 \text{ mm}$

$$\bar{x} = \frac{b^2}{2b+d} = \frac{(80)^2}{(2 \times 80) + 60} = 29.1 \text{ mm}$$

$$A = 0.707 h * (2b + d) = 0.707 * 6 * (220)$$

$$A = 933.24 \text{ mm}^2$$

$$J_u = \frac{8(80)^3 + (6 \times 80 \times 3600) + (60)^3}{12} - \frac{(80)^4}{160 + 60} = 317.15 \times 10^3 \text{ mm}^4$$

$$\therefore \tau' = \frac{F}{A} = \frac{2000}{933.24}$$

$$\boxed{\tau' = 2.14 \text{ MPa}}$$

$$\therefore \tau_c = \frac{T r}{J} = \frac{T r_c}{0.707 h J_u}$$

$$r_c = \sqrt{(50.9)^2 + (30)^2} = 59.1 \text{ mm}$$

$$T = F * (200 + 80 - \bar{x}) = 2000 * (280 - 29.1)$$

$$T = 501.8 \times 10^3 \text{ N.mm}$$

$$\tau_c = \frac{501.8 \times 10^3 * 59.1}{0.707 * 6 * 317.15 \times 10^3} = 22.04 \text{ MPa}$$

$$\Rightarrow \boxed{\tau_c = 22.04 \text{ MPa}}$$

$$\tan \theta = \frac{30}{50.9} = 0.59 \Rightarrow \theta = 30.5^\circ$$

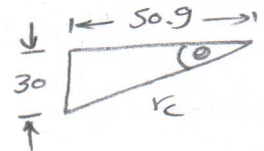
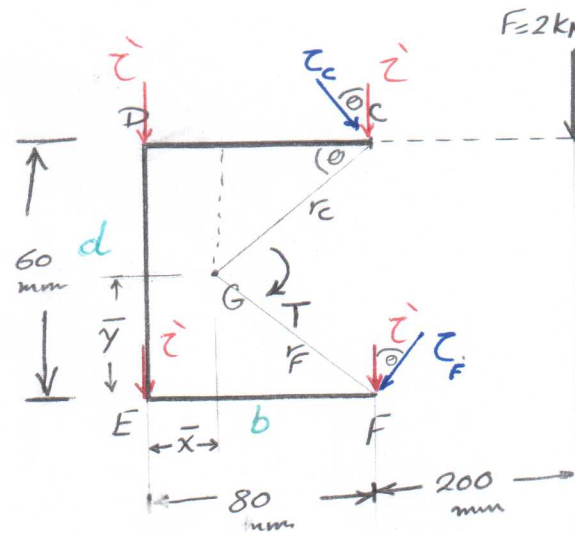
$$\tau_{max} = \sqrt{\tau'^2 + \tau_c^2 + 2\tau'\tau_c \cos \theta}$$

$$\tau_{max} = \sqrt{(2.14)^2 + (22.04)^2 + 2 * 2.14 * 22.04 * \cos 30.5}$$

$$\boxed{\tau_{max} = 24 \text{ MPa}}$$

There is no need to add another weld on CF side

as $\tau_{stress} < \tau_{max \text{ available}}$



Question (4) Plain $\hookrightarrow F_{\max} = 620 \text{ N}$ $\hookrightarrow S = 30 \text{ mm}$ $\hookrightarrow C = 6 = \frac{D}{d}$

$$\tau_{\text{all}} = 570 \text{ MPa} \quad \hookrightarrow G = 70 \times 10^3 \text{ MPa}$$

Req $\Rightarrow d \hookrightarrow K_{\text{stiffness}}$ $\hookrightarrow N \hookrightarrow \text{Solid} \hookrightarrow \text{free length}$ if $P = 8 \text{ mm}$
sol

$$\text{The Wahl factor } K = \frac{4 \times 6 - 1}{4 \times 6 - 4} + \frac{0.615}{6} = 1.25$$

$$\therefore \tau = K \frac{8FD}{\pi d^3} = K \frac{8FC}{\pi d^2}$$

$$570 = \frac{1.25 \times 8 \times 620 \times 6}{\pi d^2} \Rightarrow \boxed{d = 4.6 \text{ mm}} \quad \begin{matrix} C = \frac{D}{d} = 6 \\ \Rightarrow D = 27.6 \text{ mm} \end{matrix}$$

$$\therefore K_{\text{stiff}} = \frac{F}{\delta} = \frac{620}{30} \Rightarrow \boxed{K_{\text{stiff}} = 20.7 \text{ N/mm}}$$

$$\therefore \delta = \frac{8FD^3N}{Gd^4} \Rightarrow$$

$$N = \frac{30 \times 70 \times 10^3 \times (4.6)^4}{8 \times 620 \times (27.6)^3} \Rightarrow N = 9.02 \Rightarrow \boxed{N = 10 \text{ turns}}$$

$$\text{Solid length} = (n+1)d = 11 \times 4.6 \Rightarrow \boxed{\text{Solid length} = 50.6 \text{ mm}}$$

$$\text{Free length} = (P \times n) + d = (8 \times 10) + 4.6 \Rightarrow \boxed{\text{free length} = 84.6 \text{ mm}}$$