

Kinetics of a particle

work and energy

$$dU_{1-2} = F dr$$

$$U_{1-2} = \int_{r_1}^{r_2} F dr = \int_{s_1}^{s_2} F ds$$

$$\Sigma F_{\text{net}} = m \vec{a}$$

$$\Sigma F_{\text{net}} = m v \frac{dv}{ds}$$

$$\int_{s_1}^{s_2} \Sigma F_{\text{net}} ds = \int_{v_1}^{v_2} m v dv$$

$$U_{1-2} = \frac{1}{2} m v_2^2 - \frac{1}{2} m v_1^2$$

for work done

⊛ Const force $\int_{s_1}^{s_2} F ds = F \Delta s = F(s_2 - s_1)$

⊛ inclined force



$$U_{1-2} = F \cos \theta \Delta s$$

⊛ reverse force



$$U_{1-2} = -F \Delta s$$

⊛ tangential force

$$U_{1-2} = \int_{s_1}^{s_2} F ds = \int_{\theta_1}^{\theta_2} r F d\theta$$

⊛ Weight

$$U_{1-2} = \pm mgh \quad \begin{matrix} \text{dis} \\ \text{up} \end{matrix}$$

⊛ spring

$$U_{1-2} = \int_{s_1}^{s_2} F(s) ds = \int_{s_1}^{s_2} -Ks ds$$

$$= -K \left[\frac{s^2}{2} \right]_{s_1}^{s_2} = -\frac{1}{2} K (s_2^2 - s_1^2)$$