Fluid Mechanics

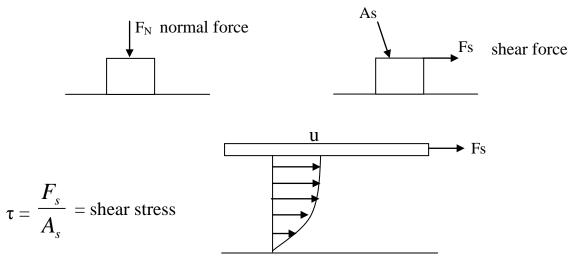
References

- 1. "Fluid Mechanics and applications" by Frank M. White.
- 2. "Fluid Mechanics", By J.F. Douglas, J.M. Grasiore, and J.A. Swaffield.
- "Fluid Mechanics Fundamentals and Applications" By Yunus A. Cengel, and John M. Cimbala.
- 4. "Fluid Mechanics and fluid power engineering" By D.S. Kumar.

<u>Fluid:</u>

The science that deals with the behavior of fluids at rest (fluid statics) or in motion (fluid dynamics) and the interaction of fluids with solids or other fluids at the boundaries.

It is a substance which deforms continuously under the action of shearing forces, however small they are. This deformation is permanent even if the force is removed.



- * Difference between solid & fluid?
- * Difference between liquid & gas?



<u>Units</u>

	B.S units	C.GS	S.I	
Force	lb _f	dyne	Ν	
mass	lb	gm	Kg	
distance	ft	cm	m	
time	S	S	S	

<u>SI units</u>

M, L, T, O Dimensions

		Dim	SI unit
	Mass	М	Kg
الوحدات الاساسية	Length	L	m
	Time	Т	S
	temperature	θ	К
	Velocity	L/T	m/s
الوحدات المشتقة	acceleration	L/T^2	m/s ²
	Force	MLt ⁻²	$kg.m/s^2 = N$
	pressure	ML ⁻¹ T ⁻²	N/m ² =Pa =kg/ms ²

(work , energy , torque) = N.m = Joule

Power =
$$\frac{N.m}{S} = \frac{J}{S} = watt$$

Units Conversion

1 ft = 0.3049 m	
$11b_{f} = 4.448 N$	& $1 \text{ N} = 10^5 \text{ dyne}$
1 kw = 1.36 HP	
1 kg = 2.2 lb	& 1 bar = 10^5 Pa
$1 \text{ kg}_{f} = 9.81 \text{ N}$	

TABLE 1-1

The seven fundamental (or primary) dimensions and their units in SI

Dimension	Unit
Length Mass Time Temperature Electric current Amount of light	meter (m) kilogram (kg) second (s) kelvin (K) ampere (A) candela (cd)
Amount of matter	mole (mol)

TABLE 1-2					
Standard prefixes i	Standard prefixes in SI units				
Multiple	Prefix				
1012	tera, T				
10 ⁹	giga, G				
10 ⁶	mega, M				
10 ³	kilo, k				
10 ²	hecto, h				
10 ¹	deka, da				
10 ⁻¹	deci, d				
10-2	centi, c				
10 ⁻³	milli, m				
10-6	micro, μ				
10 ⁻⁹	nano, n				
10 ⁻¹²	pico, p				

Primary dimension	SI unit	BG unit	Conversion factor
Mass {M}	Kilogram (kg)	Slug	1 slug = 14.5939 kg
Length $\{L\}$	Meter (m)	Foot (ft)	1 ft = 0.3048 m
Time $\{T\}$	Second (s)	Second (s)	1 s = 1 s
Temperature $\{\Theta\}$	Kelvin (K)	Rankine (°R)	$1 \text{ K} = 1.8^{\circ} \text{R}$

Force = (Mass)(Acceleration) F = ma W = mg (N) Power = T * ω $= F * r * \omega$ $= F * r * \omega$

Dimensional Homogeneity

Example

A useful theoretical equation for computing the relation between pressure, velocity, and altitude in a steady flow of a nearly inviscid, nearly incompressible fluid with negligible heat transfer and shaft work is:

 $p_0 = p + \frac{1}{2}\rho V^2 + \rho g Z$ where p_0 = stagnation pressure p = pressure in moving fluid V = velocity ρ = density Z = altitude g = gravitational acceleration

(a) Show that Eq. (1) satisfies the principle of dimensional homogeneity, which states that all additive terms in a physical equation must have the same dimensions. (b) Show that consistent units result without additional conversion factors in SI units.

	Solution			
Part (a)	(a) We can express Eq. (1) dimensionally, using braces by entering the dimensions of each from Table 1.2:			
	$\{ML^{-1}T^{-2}\} = \{ML^{-1}T^{-2}\} + \{ML^{-3}\}\{L^{2}T^{-2}\} + \{ML^{-3}\}\{LT^{-2}\}\{L\}$			
	$= \{ML^{-1}T^{-2}\}$ for all terms Ans. (a)			
Part (b)	Enter the SI units for each quantity from Table 1.2:			
	$\{N/m^2\} = \{N/m^2\} + \{kg/m^3\}\{m^2/s^2\} + \{kg/m^3\}\{m/s^2\}\{m\}$			
	$= \{N/m^2\} + \{kg/(m \cdot s^2)\}$			

Example

1.9 According to information found in an old hydraulics book, the energy loss per unit weight of fluid flowing through a nozzle connected to a hose can be estimated by the formula

 $h = (0.04 \text{ to } 0.09)(D/d)^4 V^2/2g$

where h is the energy loss per unit weight, D the hose diameter, d the nozzle tip diameter, V the fluid velocity in the hose, and g the acceleration of gravity. Do you think this equation is valid in any system of units? Explain.

$$\begin{aligned} h &= (0.04 \ t_0 \ 0.09) \left(\frac{D}{d}\right)^4 \frac{V^2}{2g} \\ \left[\frac{FL}{F}\right] &\doteq \left[0.04 \ t_0 \ 0.09\right] \left[\frac{L^4}{L^4}\right] \left[\frac{1}{2}\right] \left[\frac{L^2}{T^2}\right] \left[\frac{T^2}{L}\right] \\ \left[L\right] &\doteq \left[0.04 \ t_0 \ 0.09\right] \left[L\right] \end{aligned}$$

Since each term in the equation must have the same dimensions, the constant term (0.04 to 0.09) must be dimensionless. Thus, the equation is a general homogeneous equation that is valid in any system of units. Yes.

Example

1.12 A formula to estimate the volume rate of flow, Q, flowing over a dam of length, B, is given by the equation

 $Q = 3.09BH^{3/2}$

where H is the depth of the water above the top

of the dam (called the head). This formula gives Q in ft³/s when B and H are in feet. Is the constant, 3.09, dimensionless? Would this equation be valid if units other than feet and seconds were used?

 $Q = 3.09 \quad B \quad H^{3/2}$ $[L^{3}T^{-1}] \doteq [3.09][L][L]^{3/2}$ $[L^{3}T^{-1}] \doteq [3.09][L]^{5/2}$

Since each term in the equation must have the same dimensions the constant 3.09 must have dimensions of $L^{1/2}T^{-1}$ and is therefore not dimensionless. <u>No</u>. Since the constant has dimensions its value will change with a change in units. <u>No</u>.

Properties of fluids

- * **<u>Density</u>** : mass per unit volume $\rho = \frac{m}{V}$
 - Dim. $\frac{M}{L^3}$ for water $\rho = 1000 \text{ kg/m}^3$

* Specific weight : weight per unit volume

 $\gamma = \frac{\text{weight}}{\text{volume}} = \frac{\text{m} * \text{g}}{\text{V}} = \rho \text{g}$ Dim. $\frac{\text{ML}}{\text{T}^2} * \frac{1}{\text{L}^3}$, for water $\gamma = 1000 * 9.8$ $\frac{\text{N}}{\text{m}^3}$

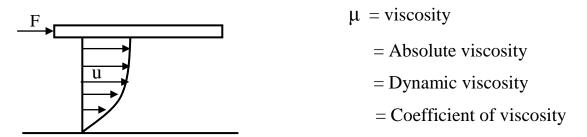
* Specific volume : volume per unit mass

 $v = \frac{volume}{mass} = \frac{1}{\rho} m^3/kg$ For water $v = 0.001 m^3/kg$

* <u>Specific gravity</u>: $SG = \frac{Sp. Weight of fluid}{Sp. Weight of water}$ $= \frac{\gamma_f}{\gamma_w} = \frac{\rho_f g}{\rho_w g} = \frac{\rho_f}{\rho_w} \quad \text{dimensionless}$ For water $SG_w = 1$

<u>* Viscosity</u> (μ): The property which causes friction between fluid and boundary or between fluid layers if they is velocity difference.

It's a property that represents the internal resistance of a fluid to motion or the "fluidity". The viscosity of a fluid is a measure of its "resistance to deformation."



$$F_{viscous} = F$$

$$F_{viscous} \quad \alpha \quad A_{friction} \quad \frac{du}{dy}$$

$$F_{vis} = Const \cdot A_{friction} \quad \frac{du}{dy}$$

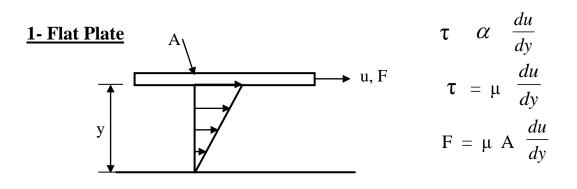
$$F_{vis} = \mu A_{friction moving} \quad \frac{du}{dy}$$
Newton's law of viscosity

 μ = coefficient of viscosity depends on type of fluid and its temperature

$$\mu = \frac{Fvis}{Afriction} * \frac{dy}{du} \qquad \text{for water } \mu = 0.001 \frac{N.s}{m^2}$$
$$= 0.01 \frac{dyne \cdot s}{cm^2}$$
$$= 0.01 \text{ poise}$$
$$= 0.01 \text{ poise}$$
$$= 1 \text{ centi poise}$$

For a small thickness of fluid layer, velocity distribution car be assumed straight

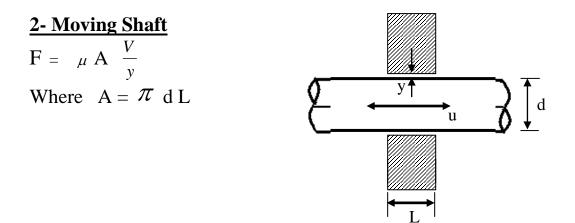
line.
$$\frac{du}{dy} = \frac{\Delta U}{\Delta y}$$

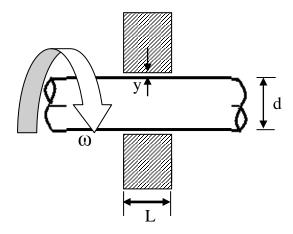


as : τ : shear stress

 μ : viscosity $\frac{du}{dy}$: rate of shear strain

F : viscous force





3- Rotating Shaft			
$F = \mu A$	<u>u</u>		
	У		
$u = \omega r$			
$r = \frac{d}{2}$			

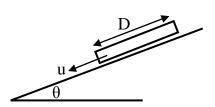
If N is given
$$\therefore \quad \omega = \frac{2\pi N}{60}$$

as N : rpm & ω : rad /sec

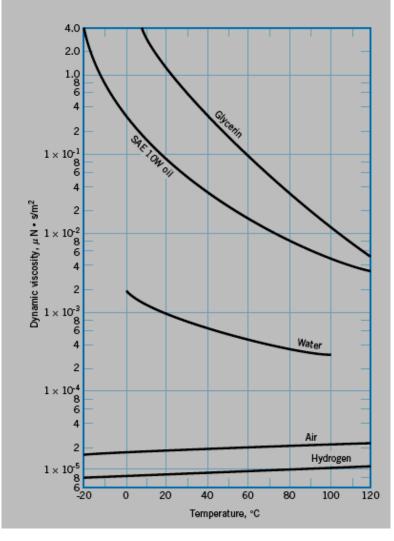
If rps <u>convert</u> ω rad/sec

 $\omega = 2\pi (rps)$

 $\frac{4 - \text{Sliding Disk}}{A = \frac{\pi}{4} D^2}$



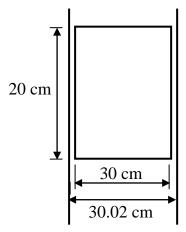
* Relation between viscosity and temperature for a certain fluid

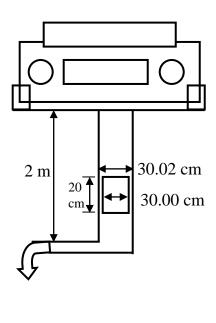


Example

For the shown position of car lifting system <u>Calculate:</u> the force required to overcome friction when the piston moves at 2m/s

take $\mu_{oil} = 0.02$ Pa.s

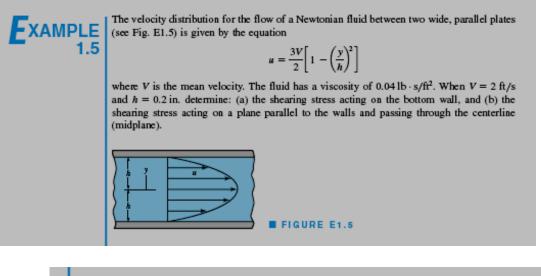




$$F_{\text{vis}} = \mu A \frac{du}{dy}$$

= 0.02 * (\pi d L) * \frac{u}{\left(\frac{D-d}{2}\right)}
= 0.02 * \left(\pi * \frac{30}{100} * \frac{20}{100\right)} * \frac{2}{\left(\frac{30.02 - 30}{200\right)}\right)}
= Newton

Example



SOLUTION_

For this type of parallel flow the shearing stress is obtained from Eq. 1.9,

$$\tau = \mu \frac{du}{dy}$$
(1)

Thus, if the velocity distribution u = u(y) is known, the shearing stress can be determined at all points by evaluating the velocity gradient, du/dy. For the distribution given

$$\frac{du}{dy} = -\frac{3Vy}{h^2}$$
(2)

(a) Along the bottom wall y = -h so that (from Eq. 2)

$$\frac{du}{dy} = \frac{3V}{h}$$

and therefore the shearing stress is

and thus the shearing stress is

$$\tau_{\text{bottom}} = \mu \left(\frac{3V}{h}\right) = \frac{(0.04 \text{ lb} \cdot \text{s/ft}^2)(3)(2 \text{ ft/s})}{(0.2 \text{ in.})(1 \text{ ft/12 in.})}$$
$$= 14.4 \text{ lb/ft}^2 \text{ (in direction of flow)}$$
(Ans

This stress creates a drag on the wall. Since the velocity distribution is symmetrical, the shearing stress along the upper wall would have the same magnitude and direction. (b) Along the midplane where y = 0 it follows from Eq. 2 that

$$\frac{du}{dy} = 0$$
(100)

From Eq. 2 we see that the velocity gradient (and therefore the shearing stress) varies linearly with y and in this particular example varies from 0 at the center of the channel to 14.4 lb/ft2 at the walls. For the more general case the actual variation will,

of course, depend on the nature of the velocity distribution.

* Kinematic viscosity (v): It is defined as the ratio of dynamic viscosity to density

$$\upsilon = \frac{\mu}{\rho} = \frac{Pa.S}{kg/m^3} = \frac{kg.m.s \ m^3}{s^2 m^2 \ kg} = (m^2/s)$$

For water $\upsilon = 0.01 \ cm^2/s$
= 0.01 stoke as stoke = cm²/s
= 1 centi stokes

*** Vapour pressure of liquids** (Pvap):

It is the pressure at which a liquid start to boil at working temperature.

Boling temp increases by increasing pressure on liquid surface.

Boling temp decreases by decreasing pressure on liquid surface.

Р	0.3	0.5	1	4	10	atm.
Boling temp	40	70	100	120	180	°C

To avoid vapor formation $P_{min} > P_{vap}$

* Bulk modulus of elasticity (k)

It's the rate at which the pressure changes with volumetric strain $(\Delta V/V)$

$$\mathbf{K} = \frac{-\Delta P}{\Delta V / V}$$

Large value of k

means that big change of pressure Causes small

change of volume

: The fluid is incompressible $k = \dots * 10^9 (P_a)$

Small value of k

means that small change of pressure causes a large change of volume

: The fluid is compressible
$$k = \dots * 10^{6} (P_a)$$

The quantity $\beta = 1/k$ is called the compressibility of the fluid.

$$1/\beta = k = \frac{-\Delta P}{\Delta V/V}$$

Notice that the greater the value of the bulk modulus of elasticity (k), the smaller the value of compressibility (β).

* Newtonian & Non - Newtonian:

$$\tau = \frac{F_{vis}}{A} = \mu \frac{du}{dy}$$

as τ : Shear stress

$$\frac{du}{dy}$$
: rate of shear strain

If
$$\tau \alpha \frac{du}{dy}$$
 $\therefore \mu = \text{const.}$ \therefore It is a Newtonian fluid

 $\mu = \text{const.}$ Newtonian fluid $\mu \quad \uparrow \downarrow \longrightarrow$ Non Newtonian

